

Register No.: Name:

SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS)

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM)

SIXTH SEMESTER B.TECH DEGREE EXAMINATION (R,S), MAY 2024

ROBOTICS AND AUTOMATION

(2020 SCHEME)

Course Code : 20RBT306

Course Name: Signals and Systems

PART A

(Answer all questions. Each question carries 3 marks)

1. Sketch the signal $x(t) = -2u(0.5t+2)$.
2. Find the even and odd components of the signal $x(t) = 1+2t+3t^2+4t^3$.
3. Find the Fourier transform of unit step signal.
4. Determine the Nyquist rate for the following signals
(i) $x(t) = 2 \text{sinc}(100\pi t)$ (ii) $x(t) = 10 \sin 40\pi t \cos 300\pi t$.
5. Using the properties of Z transform find the Z transform of the following signals
(i) $x(n) = u(-n+1)$ (ii) $2(3)^n u(-n)$.
6. State and prove differentiation in frequency domain property of DTFT.
7. Consider $x(n) = \{1, 2, -3, 0, 1, -1, 4, 2\}$ with 8 point DFT. Evaluate the following values of $X(K)$ without computing DFT
(i) $X(0)$ (ii) $X(4)$.
8. Determine the output response $y(n)$ if $x(n) = \{1, 2, 3, 1\}$ and $h(n) = \{1, 1, 1\}$.
9. Draw the basic butterfly diagram of DFT algorithm.
10. Differentiate between FIR and IIR filter.

PART B

(Answer one full question from each module, each question carries 14 marks)

MODULE I

11. a) Check the following systems are (i) static or dynamic (ii) Linear or nonlinear (iii) causal or non-causal (iv) Time-invariant or time variant (9)
(i) $y(n) = x(n)x(n-2)$ (ii) $y(n) = a^n u(n)$.
- b) Determine whether the following signals are energy signals or power signal and calculate their energy or power (5)
(i) $x(t) = \sin^2 \omega t$ (ii) $x(t) = tu(t)$.

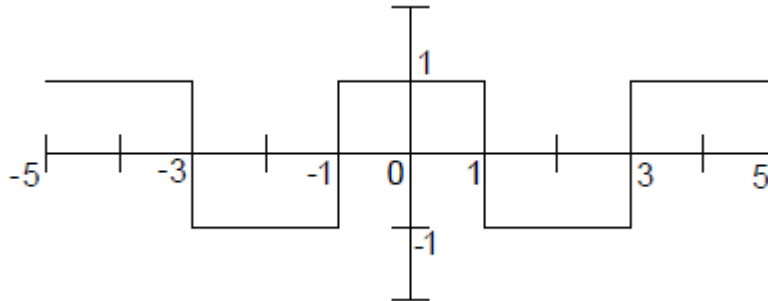
OR

12. a) Find whether the following systems are stable or not (6)
(i) $h(t) = (2+e^{-3t})u(t)$ (ii) $y(n) = x(n) + 0.5x(n-1) + 0.25x(n-2)$.

- b) Examine whether the following signals are periodic or not? If periodic determine the fundamental period (8)
- (i) $\sin 12\pi t$ (ii) $3u(t)+2 \sin 2t$ (iii) $3 \sin 200\pi t + 4 \cos 100t$
- (iv) $\cos\left(\frac{n}{6}\right)\cos\left(\frac{n\pi}{6}\right)$ (v) $\sin\frac{2\pi n}{3} + \cos\frac{2\pi n}{5}$.

MODULE II

13. a) Obtain the trigonometric Fourier series for the wave form shown in the below figure. (9)



- b) State and Prove Parseval's relation. (5)

OR

14. a) State and prove sampling theorem for low pass signal. (9)
- b) Find the Fourier transform of the following (5)
- (i) $te^{-at}u(t)$ (ii) $\cos \omega_0 t u(t)$.

MODULE III

15. a) Find the Z-transform and ROC of the following signals (9)
- (i) $x(n)=\left(\frac{1}{2}\right)^n u(n-2)$ (ii) $a^n u(n)-b^n u(n-1)$.
- b) Write the properties of ROC. (5)

OR

16. a) Consider a discrete time LTI system with impulse response $h(n)=(1/2)^n u(n)$. Use Discrete Time Fourier Transform(DTFT) to determine the response to the signal $x(n)=(3/4)^n u(n)$. (9)
- b) Using the properties of DTFT find the DTFT of the following. (5)
- (i) $u(n+1)-u(n-2)$ (ii) $n 3^{-n} u(-n)$.

MODULE IV

17. a) Find the output of the sequence for the given $h(n)$ and $x(n)$ using overlap save method (9)
- $x(n)=\{1,2,-1,2,3,-2,-3,-1,1,1,2,-1\}$ $h(n)=\{1,2\}$.
- b) Find the circular convolution of the sequence $x_1(n)=\{1,-1,-2,3,-1\}$ (5)
- $x_2(n)=\{1,2,3\}$.

OR

18. a) Compute the 8-point DFT of the sequence given below (10)
- $x(n)=1$ $0 \leq n \leq 3$

$$0 \leq n \leq 7.$$

- b) Find the IDFT of $Y(K) = \{1, 0, 1, 0\}$. (4)

MODULE V

19. a) Find the DFT of the give sequence $x(n)$ using DIT algorithm. (10)
 $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$.

- b) Draw the direct form structure of the FIR system described by the transfer function (4)

$$H(z) = 1 + \frac{1}{2}z^{-1} + \frac{3}{8}z^{-2} + \frac{5}{4}z^{-3} + \frac{1}{2}z^{-4} + \frac{7}{8}z^{-5}.$$

OR

20. a) Obtain the direct form I, II of the IIR system described by the difference equation (10)

$$y(n) = -\frac{3}{8}y(n-1) + \frac{3}{32}y(n-2) + \frac{1}{64}y(n-3) + x(n) + 3x(n-1) + 2x(n-2).$$

- b) Obtain the IDFT of the following sequence $X(K) = \{6, -2+2j, -2, -2-2j\}$ using DIF algorithm. (4)