

Register No.: Name:

SAINTGITS COLLEGE OF ENGINEERING (AUTONOMOUS)

(AFFILIATED TO APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY, THIRUVANANTHAPURAM)

FIFTH SEMESTER INTEGRATED MCA DEGREE EXAMINATION (S), FEBRUARY 2024 (2020 SCHEME)

Course Code: 20IMCAT301

Course Name: Numerical Methods

Max. Marks: 60

Duration: 3 Hours

Non-programmable calculator may be permitted in the examination hall.

PART A

(Answer all questions. Each question carries 3 marks)

1. Determine the orders of the following matrices and perform the indicated operations on the matrices:

$$A = \begin{bmatrix} 5 & 1 \\ 7 & 3 \\ -2 & -1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ 3 & 2 \end{bmatrix}, C = [1 \ 2 \ 0 \ 3]$$

- (i) AB
- (ii) 7A
- (iii) 3C

2. Evaluate the expression $(A-I)(A+2I)$ for the matrix $A = \begin{bmatrix} 3 & 5 \\ -2 & 4 \end{bmatrix}$.
3. Determine whether the set $\{[1 \ 1], [1 \ -1]\}$ is linearly independent.
4. Find the rank of the matrix $A = \begin{bmatrix} 1 & 2 & 4 & 2 \\ 1 & 1 & 3 & 2 \\ 1 & 4 & 6 & 2 \end{bmatrix}$.
5. Find the eigen values of the matrix $A = \begin{bmatrix} 8 & -4 \\ 2 & 2 \end{bmatrix}$.
6. Find the eigen values of A^{-1} if the matrix A is $\begin{bmatrix} 2 & 5 & -1 \\ 0 & 3 & 2 \\ 0 & 0 & 4 \end{bmatrix}$.
7. Define principle of least squares.
8. What are the normal equations for fitting of a parabola $y = a + bx + cx^2$.
9. Explain Lagrange's interpolation formula.
10. Estimate the value of $y(2)$ from the following data using Lagrange's interpolation formula:

x	1	3	4
y	1	27	64

PART B

(Answer one full question from each module, each question carries 6 marks)

MODULE I

11. a) Define singular and non-singular matrices. Find the inverse of the

$$\text{matrix } A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 2 \end{bmatrix}. \quad (2)$$

- b) Find the inverse of the matrix, if exists, $A = \begin{bmatrix} 2 & 0 & -1 \\ 0 & 1 & 2 \\ 3 & 1 & 1 \end{bmatrix}$ using Gauss-Jordan method. (4)

OR

12. a) Define a diagonal matrix with example. (2)

- b) Evaluate the expression $(I - A)(A^2 - I)$ for the matrix (4)

$$A = \begin{bmatrix} 2 & -1 & 1 \\ 3 & -2 & 1 \\ 0 & 0 & 1 \end{bmatrix}.$$

MODULE II

13. a) Determine whether the values $x = 1, y = -3, z = 2$ are solution to the system

$$\begin{aligned} x + y + 2z &= 2 \\ x - y - 2z &= 0 \\ x + 2y + 2z &= 1 \end{aligned} \quad (1)$$

- b) Use Gaussian elimination method to solve the system of equations:

$$\begin{aligned} y - 2z &= 4 \\ x + 3y + 2z &= 1 \\ -2x + 3y + z &= 2 \end{aligned} \quad (5)$$

OR

14. Determine the number of solutions to the system

$$\begin{aligned} 2x - 3y + z &= -1 \\ x - y + 2z &= 2 \\ 2x + y - 3z &= 3 \end{aligned} \quad (6)$$

Hence find the solution.

MODULE III

15. Find the eigen values and eigen vectors of the matrix $A = \begin{bmatrix} 3 & 1 & -1 \\ -2 & 1 & 2 \\ 0 & 1 & 2 \end{bmatrix}$. (6)

OR

16. Diagonalize the Matrix $A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$. (6)

MODULE IV

17. Apply method of least squares to fit an equation of the form $y = ax + b$ to the following data:

x	0.5	1.1	1.5	2.1	2.3	(6)
y	32	3	34.2	35.1	35.7	

OR

18. Analyze the following data to fit a curve of the form $y = a + bx^2$.

x	1	2	3	4	5	6	(6)
y	0.56	0.89	1.04	1.63	2.95	4.5	

MODULE V

19. Estimate the value of $y(3)$ from the following data, using Lagrange's interpolation formula:

x	0	1	2	4	5	6	(6)
y	1	14	15	5	6	19	

OR

20. Using Newton's forward interpolation formula, estimate the value of $\sin 8^\circ$ for the following data:

θ	5	10	15	20	25	30	(6)
$\sin \theta$	0.0871	0.1736	0.2588	0.342	0.4226	0.5	
