## B.Sc DEGREE (CBCS) REGULAR / IMPROVEMENT / REAPPEARANCE EXAMINATIONS, JANUARY 2023 <br> Third Semester

B.Sc Psychology Model I

# COMPLEMENTARY COURSE - ST3CMT23 - PROBABILITY AND PROBABILITY DISTRIBUTIONS 

2017 Admission Onwards

8E23CB8B

Time: 3 Hours

Part A<br>Answer any ten questions.<br>Each question carries 2 marks.

1. What is the frequency definition of probability?
2. $A$ and $B$ are two events such that $P(A)=.3, P(B)=0.25, P(A \mid B)=0.5$ then find $P(B \mid A)$
3. If $P(A)=0.6, P(B)=0.3, P(A \cap B)=0.1$, find the probability of neither $A$ nor $B$ will occur.
4. State the multiplication theorem for 3 independent events.
5. Give an example of a random variable.
6. What is the difference between pmf and pdf?
7. What do you mean by expectation of a random variable?
8. If $E(X)=3$ and $E(Y)=4$, then $E(X+Y)$ is
9. If $X \sim B(10,0.5)$ the $P(X=10)=$
10. If $X \sim N(10,4)$, explain the standardisation of $X$
11. If $X \sim N(0,1)$ then $P(X>0)=$
12. If $X$ is distributed as standard normal then $P(X>0)=$

## Part B

Answer any six questions.
Each question carries 5 marks.
13. Explain the terms random experiment, sample space and events with suitable example.
14. Differentiate between classical and frequency definitions of probability.
15. If A and B are independent events then Show that $A$ and $B^{c}$ are also independent.
16. The pdf of discrete random variable is given by $f(x)=k x^{2}, x=1,2,3$ find the value of k . also find its mean.
17. The discrete random variable $X$ can take values 1,2 and 3 for these values the cumulative distribution function is given by $F(x)=\frac{x^{3}+k}{40}$, show that k=13
18. Explain the variance of a random variable and state its properties.
19. Write a real life situation where binomial distibution can apply, and explain its application.
20. If $X \sim B(5,0.5)$ draw the probability mass function of $X$.
21. Explain normal distribution and state any four properties of it.

## Part C <br> Answer any two questions.

Each question carries 15 marks.
22. State and prove addition theorem in probability.
23. If a random variable $X$ possesses the following function.

| $X$ | 3 | 2 | 1 | 0 | -1 | -2 | -3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $P(X)$ | 0.1 | 0.2 | $3 k$ | $k$ | $2 k$ | 0 | 0.1 |

i) Find the value of $k$
ii) $E(X)$
iii) $V(X)$
24. In a city, it is estimated that the maximum temperature in June is normally distributed with a mean of $23^{\circ}$ and a standard deviation of $5^{\circ}$. Calculate the number of days in this month in which it is expected to reach a maximum of between $21^{\circ}$ and $27^{\circ}$.
25. The length of human pregnancies from conception to birth approximates a normal distribution with a mean of 266 days and a standard deviation of 16 days.
i) What proportion of all pregnancies will last between 240 and 270 days
ii) What length of time marks the shortest $70 \%$ of all pregnancies
iii) What length of time marks the shortest $10 \%$ of all pregnancies

