

Name:.....  
Reg. No:.....

**A**

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY**

FIRST SEMESTER M.TECH DEGREE EXAMINATIONS, DECEMBER 2018

Branch: Civil Engineering

(Specialization: Geomechanics and Structures)

**04CE 6301 - Applied Mathematics for Civil Engineers**

(Note: Non-programmable calculators may be permitted)

Time: Three hrs

Max. Marks: 60

**PART A**

*(Answer all questions. Each question carries 3 marks)*

1. Calculate the Bessel's function  $\mathcal{J}_{1/2}(x)$ . (3)
2. Find  $\mathcal{L}(t \sin at)$ . (3)
3. Develop the first order general contravariant Tensor of rank 1. (3)
4. Form the dynamic equation corresponding to  $y(x) = \int_0^x (x+t)y(t)dt + 1$ . (3)
5. Solve  $r = t$  using Monges Method. (3)
6. Using d Alembert's method find the deflection of a beam of unit length having fixed ends with initial velocity zero and initial deflection  $f(x) = kx$ . (3)
7. Evaluate the area bounded by a surface  $\frac{1}{1+x^2}$  in  $(0, 1)$  numerically with six partitions. (3)
8. Solve  $20x + y - 2z = 17, 3x + 20y - z = -18, 2x - 3y + 20z = 25$  using Gauss- Siedal iterative method. (3)

**PART B**

*(Answer all questions. Each full question carries 6 marks)*

9. Solve the Bessel's equation  $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + (x^2 - n^2)y = 0$  (6)

OR

10. (a) Prove that  $(1 - 2xt + t^2)^{-1/2} = \sum_{n=0}^{\infty} t^n P_n(x)$ , where  $P_n(x)$  represents the Legendre Polynomial. (3)  
(b) Express  $x^4 + 3x^3 - x^2 + 5x - 2$  in terms of Legendre Polynomials. (3)
11. (a) Find the Fourier transform of  $f(x) = \begin{cases} 1 & ; |x| < 1 \\ 0 & ; |x| > 1 \end{cases}$  (3)  
(b) Show that  $\mathcal{F}_s(xf(x)) = -\frac{d}{ds} \mathcal{F}_c(s)$ . (3)

OR

12. (a) Find  $\mathcal{L}\left(\frac{\cos at - \cos bt}{t}\right)$  (3)

(b) Solve  $y''' + 2y'' - y' - 2y = 0$ , where  $y(0) = y'(0) = 0, y''(0) = 6$ . (3)

13. (a) Show that  $a_{ij}A^{kj} = \Delta\delta_i^k$ , where  $\Delta$  is the determinant and  $A^{ij}$  s are cofactors of  $a_{ij}$ . (3)

(b) Expand the sum  $a_{ij}x^j$  using the summation principle. (3)

OR

14. (a) Prove that the following transformation  $T$  is admissible and find their respective inverse. (3)

$$T = \begin{cases} y^1 &= x^1 \sin x^2 \cos x^3 \\ y^2 &= x^1 \sin x^2 \cos x^3 \\ y^3 &= x^1 \cos x^3 \end{cases}$$

(b) Develop the covariant and contravariant tensors with suitable mathematical analogy. (3)

15. (a) Show that  $y = 2 - x$  is a solution of  $\int_0^x e^{x-t}y(t)dt = e^x + x - 1$ . (3)

(b) Solve  $y(x) = 3x^2 + \int_0^x \cos(x-t)y(t)dt$ . (3)

OR

16. (a) Solve  $\frac{dy}{dx} + 3y + 2 \int_0^x ydx = x$ , where  $y(0) = 0$ . (3)

(b) Using the method of successive approximation, solve the Fredholm integral equation (3)

$$y(x) = 1 + x + \int_0^x (x-t)y(t)dt$$

17. (a) Solve by Monges method  $(x - y)(xr - ys + yt) = (x + y)(p - q)$  (3)

(b) Using d' Alembert's method, find the deflection of a vibrating string of unit length having fixed ends, with initial velocity zero and initial deflection  $f(x) = a(x - x^2)$ . (3)

OR

18. An infinitely long plane uniform plate is bounded by two parallel edges and an end at right angle to them. The breadth is  $\pi$ ; this end is maintained at a temperature  $u_0$  at all points and other edges are at zero temperature. Determine the temperature at any point  $x$  of the plate in the steady-state. (6)

19. (a) Solve (3)

$$x + 4y - z = -5$$

$$x + y - 6z = -12$$

$$3x - y - z = 4$$

(b) Solve the system of non-linear equations (3)

$$x^2 + y = 11$$

$$y^2 + x = 7$$

OR

20. (a) Solve using Gauss-Siedal iteration method (3)

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$

(b) A solid of revolution is formed by rotating about the  $x$ -axis, the area between the  $x$ - axis, the lines  $x = 0$  and  $x = 1$  and the curve through the points with the following co-ordinates (3)

x:	0.00	0.25	0.50	0.75	1.00
y:	1.0000	0.9896	0.9589	0.9089	0.8415