

- 5. Hagen Poiseuille equation Derivation 10 mark
- 6. Bernoulli's equation 2 marks

$$Q=a_1 v_1 = a_2 v_2 = 5400 L/min = 0.09 m^3/s$$

$$\begin{split} V_1 &= 0.079 \text{ m/s}, V_2 &= 0.319 \text{ m/s}, \text{ Slope} = 1 \text{ in } 100 \\ \tan\theta &= 1/100 = 0.01 \quad \theta = 0.572^{\circ} \\ Z_1 &= 3\text{m}, Z_2 &= 0 \\ P_1/\rho g + V_1^{-2}/2g + Z_1 &= P_2/\rho g + V_2^{-2}/2g + Z_2 \end{split}$$

 $P_2 = 98.046 \text{ kPa}$ 

Pressure at the lower end.

8 mark

7. Vmax = 2 m/s Average velocity, V = Vmax/2 = 1m/s Re =  $\rho$  V d/ $\mu$  Flow is Laminar Pressure gradient in the direction of flow,  $\Delta P/L = 32\mu V/d^2 N/m^2$  per m length of pipe shear stress at the pipe wall,  $\tau = (\Delta P/L) r/2 N/m^2$ velocity at a distance 30 mm from the wall = (1/8 $\mu$ ) ( $\Delta P/L$ )r<sup>2</sup> m/s

Average velocity 2 marks

(i) the pressure gradient in the direction of flow (ii) shear stress at the pipe wall; (iii) Reynold's number; and (iv) velocity at a distance 30 mm from the wall. (4 x 2=8 marks),

8. Sketch of venturimeter 2 marks Bernoulli's equation 2 marks

Rate of flow - Derivation 6 marks

## PART C

## Answer any four full questions, each carries 10marks.

9. boundary layer 2marks

Sketch 3 marks

Illustration 5 marks

- 10. Sketch 2 marks, Boundary Layer Thickness Laminar Boundary Layer Turbulent boundary Layer Laminar Sub Layer (2x4 = 8 marks)
- 11. Re = VL/ $\upsilon$  = 400000, laminar 1 mark Blassius relations 1 mark each (1x3 = 3 marks) (a) Boundary layer thickness at the end of the plate  $\delta = 5x/\sqrt{Re} = 7.906x10^{-3} \text{ m}$ (b) Shear stress at the middle of the plate  $\tau = 0.332\rho U^2/\sqrt{Rex} = 0.0321 \text{ N/m}^2$ , x = 0.5 m (c) Total drag per unit length on the sides of the plate,  $C_D = 1.328/\sqrt{Re} = 2.0997x10^{-3}$

 $F_D = (1/2 \rho A U^2) \times C_D = 0.04535 N$ 

Answer  $(3 \times 2 = 6 \text{ marks})$ 

12. Buckingham's  $\pi$  theorem 3 marks , Relation 7 marks  $\Delta P = f(D, L, \rho, \mu, V, K)$ 

n = 7, m = 3, n-m = 7 - 3 = 4f (\pi 1, \pi 2, \pi 3, \pi 4) = 0, \pi 1 = \Delta P / \rho V^2, \pi 2 = \frac{L}{D}, \pi 3 = \pi / \rho VD, \pi 4 = K/D

13. Hydraulic similarities 3 types 3 marks

Explanations 7 marks

14. Model law- 3 marks Lp/Lm= 40/2.5 Froude's model law (Fe)<sub>model</sub>= (Fe)<sub>prototype</sub> [V/ $\sqrt{(gL)}$ ]<sub>model</sub>= [V/ $\sqrt{(gL)}$ ]<sub>prototype</sub>, L<sub>p</sub>/L<sub>m</sub> V<sub>p</sub>/V<sub>m</sub> = / $\sqrt{(\frac{Lp}{Lm})}$ velocity of prototype, V<sub>p</sub> 3 marks  $\rho_p/\rho_m = 1025/1000$ Fp/Fm = ( $\rho L^2 V^2$ )<sub>prototype</sub> / ( $\rho L^2 V^2$ )<sub>model</sub> Force required to drive the prototype , Force - 4 marks